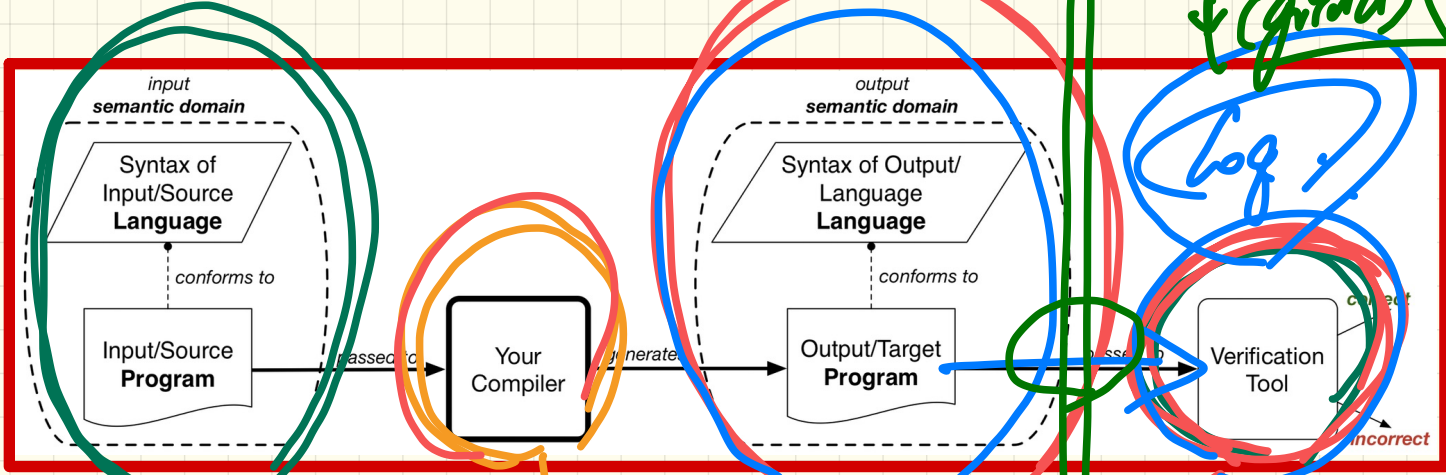


LECTURE 13

MONDAY, FEBRUARY 24

Project: Problem

Automated →



(end)
(ground)

Log

Program

≡

QuilK4

syntax-checker
type-checker

Milestones of the Project

1. Confirm Team Member(s) and the Target Verification Tool

By the end of **Tuesday, March 3**, submit a plain text file `team.txt` for your team via the Prism account of a member:

```
submit 4302 Project team.txt
```

2. Demonstrate Proficiency with the Chosen Target Verification Tool

[3%]

- On **Thursday, March 5** or **Friday, March 6** (about 2 weeks after the project is released), your team is required to meet with Jackie and demonstrate that you are familiar with the verification tool (and its specification language) you choose.
- During the meeting, you must demonstrate (using your computer) **5 non-trivial examples** (ones that show the various target language features that are relevant to your compilation) of verification. For each example, you will demonstrate how to verify it using the tool.
- **In this meeting, Jackie may suggest specific tasks that your team should complete and will be included in the evaluation of the second milestone.**

3. Demonstrate Satisfactory Progress on the Compiler

[5%]

- On **Thursday, March 19** or **Friday, March 20** (about 1 month after the project is released), your team is required to meet with Jackie and demonstrate a working version of your compiler on the following basic features of the source language features (of syntax of your own design), including:
 - variable declarations
 - variable assignments
 - variable references (i.e., referring to declared variables in expressions)
 - arithmetic, relational, and logical expressions
 - conditionals
 - specification (e.g., preconditions, postconditions, invariants, property assertions) in input programs that guide the target verification
- During the meeting, you must demonstrate (using your computer) **5 non-trivial examples** (ones that show the above source language features) of verification. For each example, you will demonstrate how to verify it using your compiler (e.g., given an input file, your tool will compile it into another file which can be taken as input by the target verification tool).
- **In this meeting, Jackie may suggest specific tasks that your team should complete and will be included in the evaluation of the final project in April.**

These two milestones are meant to make sure that you are on the right track. Based on your demo, Jackie will give you feedback.

Project: Milestones

April 6

Project: Verification Tool

You must use the ANTLR4 Parser Generator (for Java) to build your compiler.

For the target verification tool, you must choose from one of the following (and confirm by the due date; see Section 7), where a suggested starting point is provided for each tool:

• PVS

<https://pvs.csl.sri.com/>

◦ This tool is available in Prism and used by *EECS4312 Software Engineering Requirements*.

◦ More info here: <https://wiki.eecs.yorku.ca/project/sel-students/p:tutorials:pvs:start>

• Coq

<https://coq.inria.fr/>

• Isabelle

<https://isabelle.in.tum.de/>

• Alloy

<https://alloytools.org/>

• FAT

<https://pat.comp.nus.edu.sg/>

• Spin

<http://spinroot.com/spin/whatispin.html>

• Z3

<https://rise4fun.com/z3/tutorial>

Nonetheless, if there is a particular verification tool which you prefer to working with but it is not in the above list, speak to Jackie by the due date of submitting the **team.txt** file (See Section 7 for the due date).

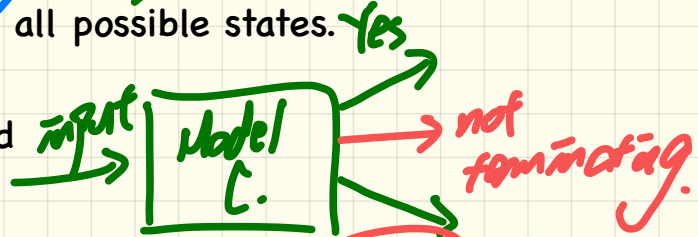
Paradigms of Verification (1)

Model checking

- A transition graph is built based on all possible states.
- An algorithm is run to ensure that certain properties are satisfied
- Automated
- **State Explosion:**

not terminating if the state space is huge
(combinatorial on sizes of variable domains)

→ LTL → ...
→ CTL → ...



Example:

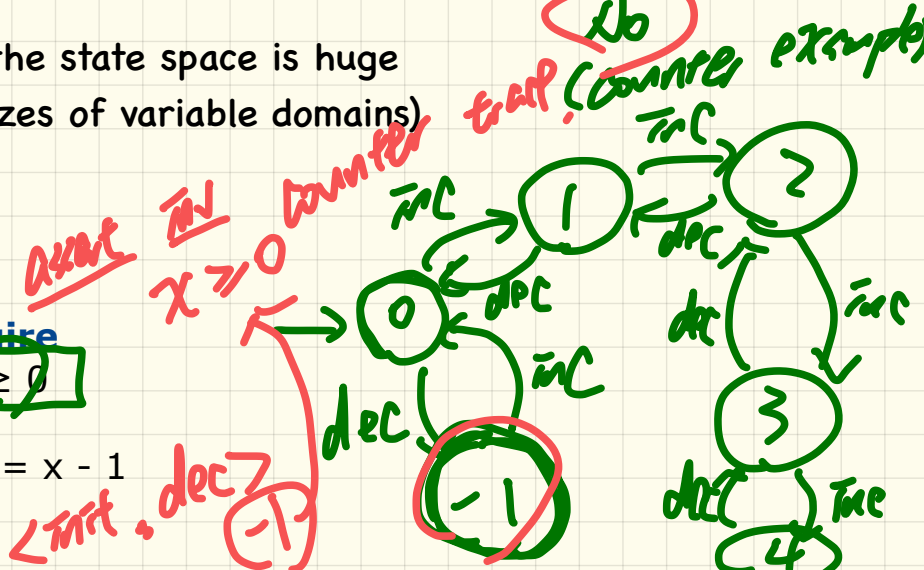
```

inc
  require
    x < 5
do
  x := x + 1
end
  
```

```

dec
  require
    x ≥ 0
do
  x := x - 1
end
  
```

WT.



Paradigms of Verification (2)

Theorem Proving

- System is encoded as predicates (e.g., Hoare Triples in EECS3311)
- A proof system of deductions (axioms, lemmas) is used to prove that the system entails certain properties.
- Manual (EECS1090 proofs on a computer)
- Complete input domains of variables can be encoded.

TAC
 $x := x + 1$

Example:

swap
require
 $x > y$
 $\{$
temp := x; x := y; y := temp
ensure
 $y > x$
end

$wp(S, y > x)$
 $x > y \Rightarrow$

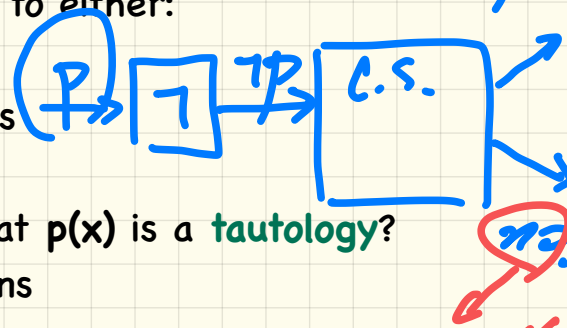
Example:

Given $\neg(\neg p) \equiv p$
 $p \Rightarrow q \equiv \neg p \vee q$
Prove: $\neg p \Rightarrow q \equiv p \vee q$
 $\equiv \text{< def. of } \Rightarrow \text{>}$
∴

Paradigms of Verification (3)

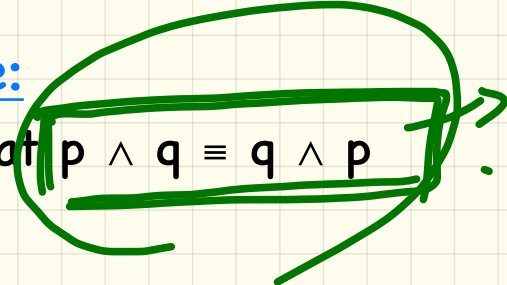
Constraint Solving

- System is encoded as predicates (e.g., Hoare Triples in EECS3311)
- Given predicate $p(x)$, an algorithm is used to either:
 - (1) find a witness x s.t. $p(x)$ is **true**.
 - (2) report that no such witness exists
- **Automated**
- How do we then use a solver to **prove** that $p(x)$ is a **tautology**?
- Combinatorial Explosion on Variable Domains



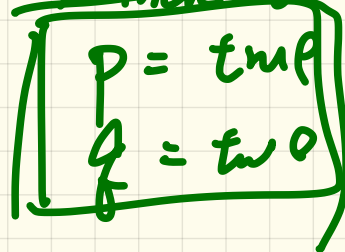
Example:

Prove that $p \wedge q \equiv q \wedge p$

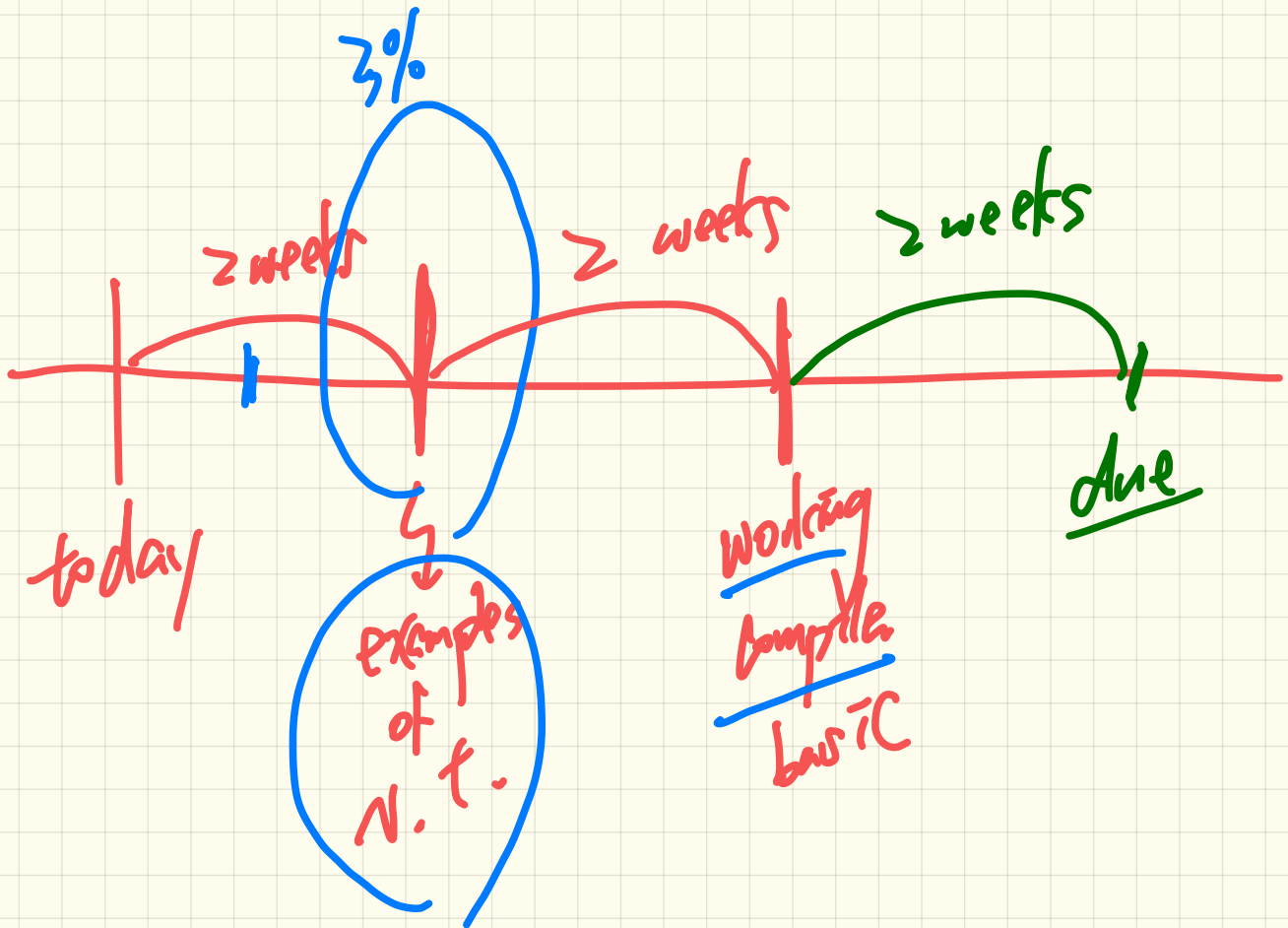


\exists

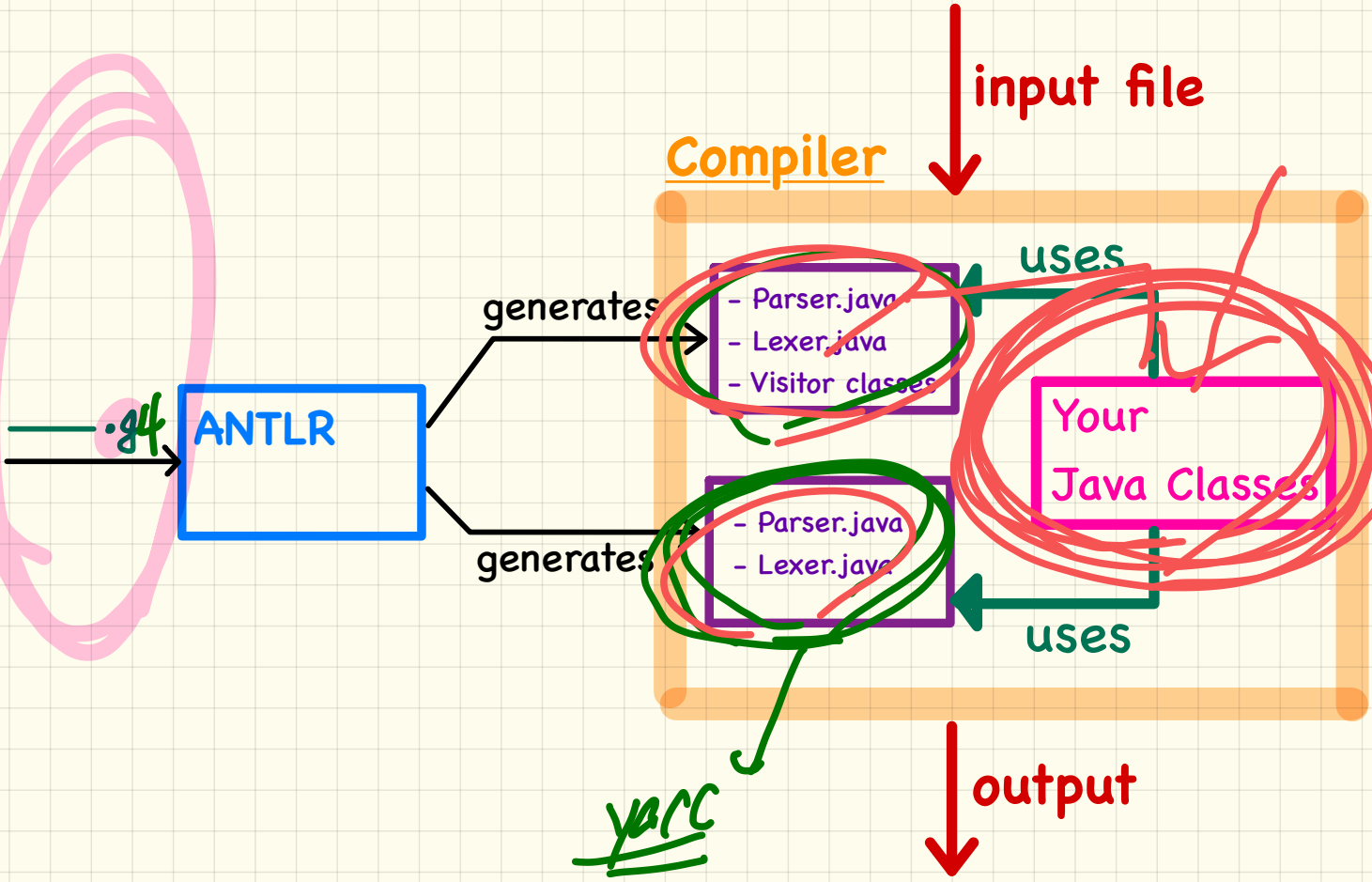
there is a

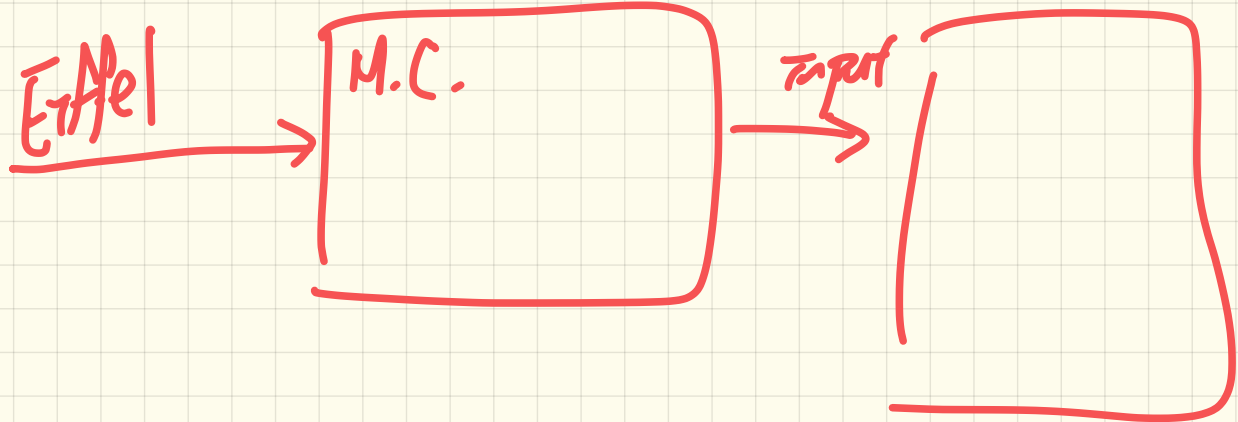


no witness for (model) witness
 $\neg P$

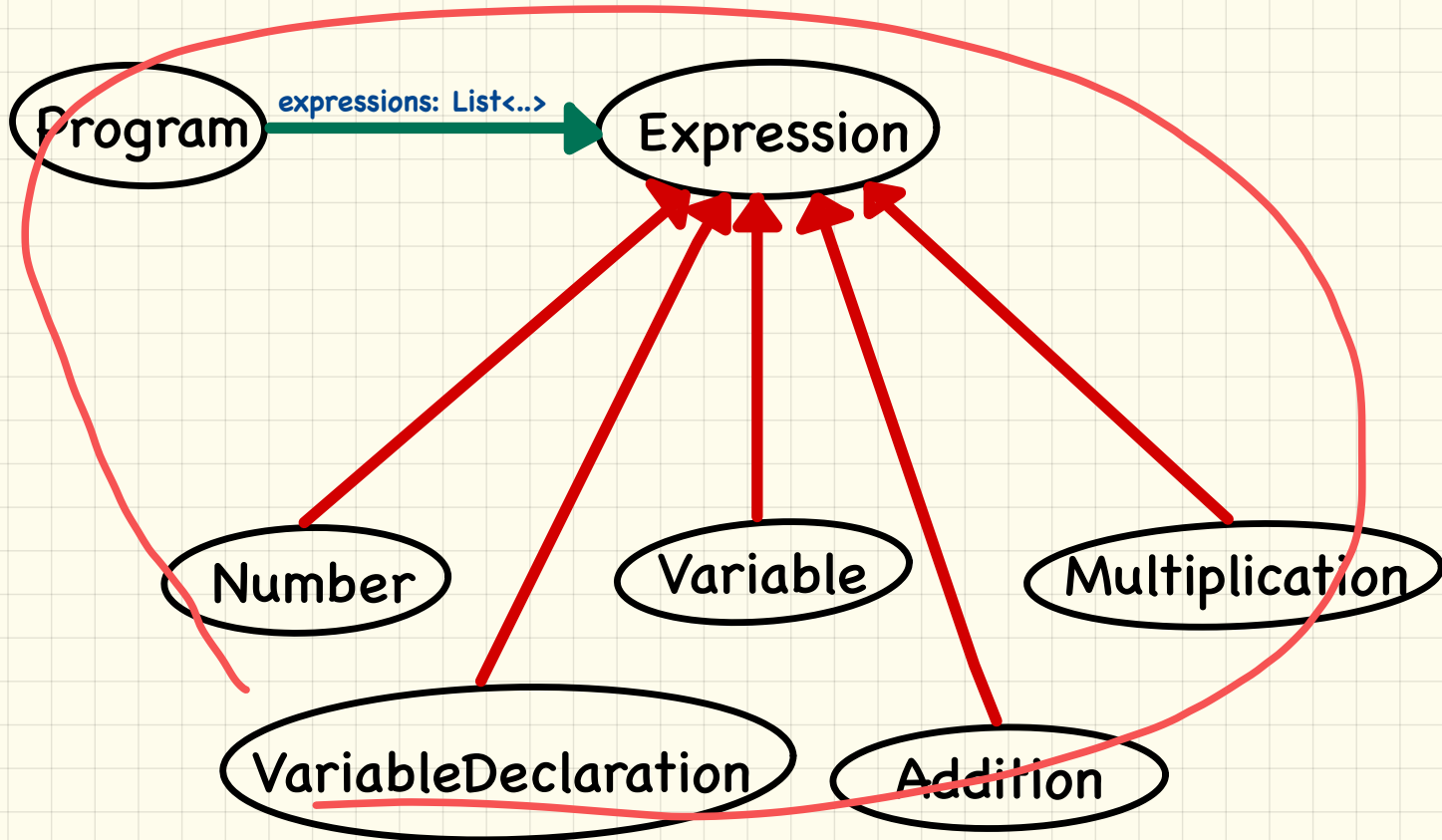


ANTLR (ANother Tool for Language Recognition)





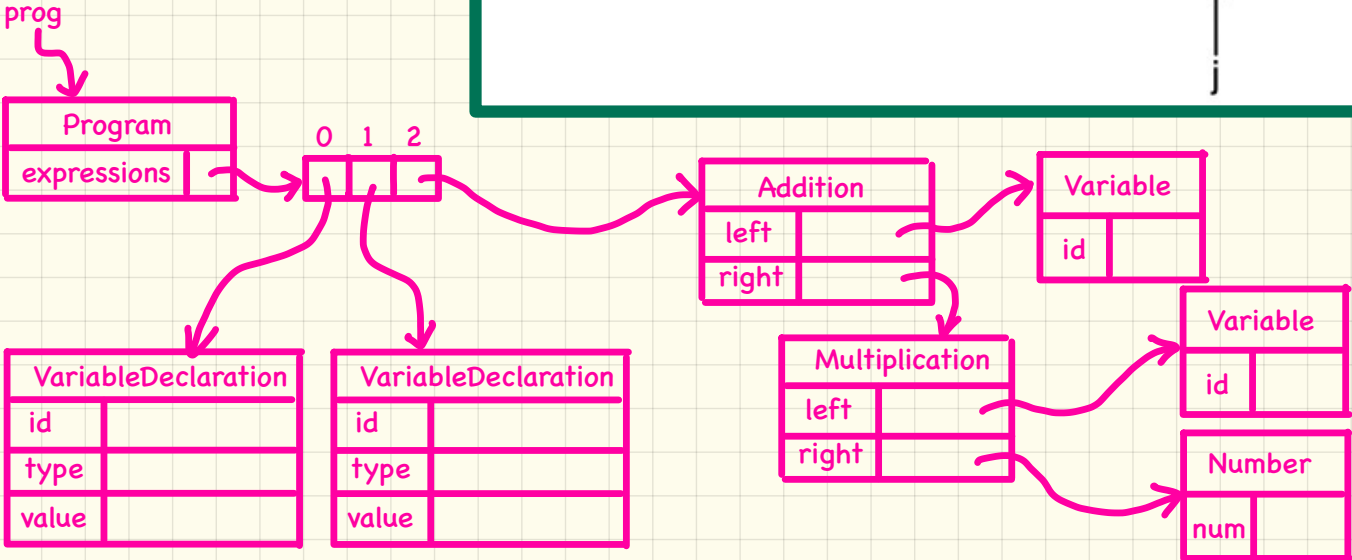
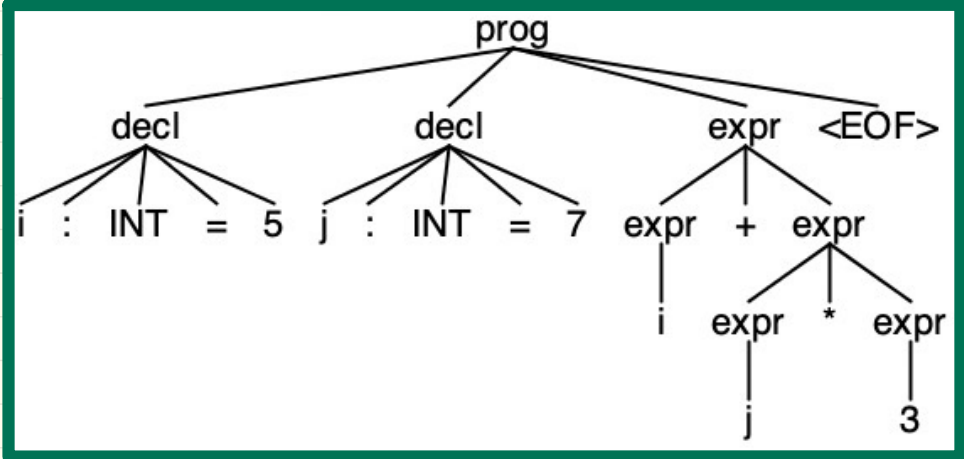
Composite Pattern of Model Classes



Building Model Objects from Parse Trees

```

i : INT = 5
j : INT = 7
i + j * 3
    
```



Backtrack-Free Grammar

$$\mathbf{FIRST}^+(A \rightarrow \beta) = \begin{cases} \mathbf{FIRST}(\beta) & \text{if } \epsilon \notin \mathbf{FIRST}(\beta) \\ \mathbf{FIRST}(\beta) \cup \mathbf{FOLLOW}(A) & \text{otherwise} \end{cases}$$

$\mathbf{FIRST}(\beta)$ is the extended version where β may be $\beta_1\beta_2\dots\beta_n$

$A \rightarrow \gamma_1 \mid \gamma_2 \mid \dots \mid \gamma_n$ satisfying:

$$\forall i, j: 1 \leq i, j \leq n \wedge i \neq j \bullet \mathbf{FIRST}^+(\gamma_i) \cap \mathbf{FIRST}^+(\gamma_j) = \emptyset$$

Top-Down Parsing: Algorithm

backtrack \triangleq pop *focus*.siblings; *focus* := *focus*.parent; *focus*.resetChildren

with **lookahead**

ALGORITHM: *TDParse*

INPUT: CFG $G = (V, \Sigma, R, S)$

OUTPUT: Root of a Parse Tree or Syntax Error

PROCEDURE:

root := a new node for the start symbol *S*

focus := *root*

initialize an empty stack *trace*

trace.push(null)

word := NextWord()

while (true):

if *focus* $\in V$ then % use FOLLOW set as well:

if \exists unvisited rule *focus* $\rightarrow \beta_1\beta_2\dots\beta_n \in R$ \wedge **word** \in FIRST'(β) **then**

create $\beta_1, \beta_2, \dots, \beta_n$ as children of *focus*

trace.push($\beta_n\beta_{n-1}\dots\beta_2$)

focus := β_1

else

if *focus* = *S* then **report syntax error**

else **backtrack**

elseif *word* matches *focus* then

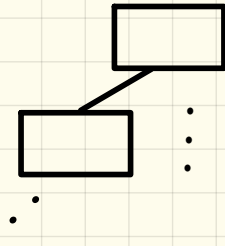
word := NextWord()

focus := *trace*.pop()

elseif *word* = EOF \wedge *focus* = null then **return root**

else **backtrack**

0	Goal	\rightarrow	Expr
1	Expr	\rightarrow	Term Expr'
2	Expr'	\rightarrow	+ Term Expr'
3			- Term Expr'
4			ϵ
5	Term	\rightarrow	Factor Term'
6	Term'	\rightarrow	\times Factor Term'
7			\div Factor Term'
8			ϵ
9	Factor	\rightarrow	(Expr)
10			num
11			name



Term'

Backtrack-Free Grammar: Exercise

$$\mathbf{FIRST}^+(A \rightarrow \beta) = \begin{cases} \mathbf{FIRST}(\beta) & \text{if } \epsilon \notin \mathbf{FIRST}(\beta) \\ \mathbf{FIRST}(\beta) \cup \mathbf{FOLLOW}(A) & \text{otherwise} \end{cases}$$

$\mathbf{FIRST}(\beta)$ is the extended version where β may be $\beta_1\beta_2\dots\beta_n$

$A \rightarrow \gamma_1 \mid \gamma_2 \mid \dots \mid \gamma_n$ satisfying:

$$\forall i, j: 1 \leq i, j \leq n \wedge i \neq j \bullet \mathbf{FIRST}^+(\gamma_i) \cap \mathbf{FIRST}^+(\gamma_j) = \emptyset$$

Is the following CFG **backtrack free**?

11	<i>Factor</i>	→	name
12			name [<i>ArgList</i>]
13			name (<i>ArgList</i>)
15	<i>ArgList</i>	→	<i>Expr MoreArgs</i>
16	<i>MoreArgs</i>	→	, <i>Expr MoreArgs</i>
17			ε

Left-Factoring: Removing Common Prefixes

Identify a common prefix α :

$$A \rightarrow \alpha \beta_1 \mid \alpha \beta_2 \mid \dots \mid \alpha \beta_n \mid \gamma_1 \mid \gamma_2 \mid \dots \mid \gamma_j .$$

[each of $\gamma_1, \gamma_2, \dots, \gamma_j$ does not begin with α]

Rewrite that production rule as:

$$\begin{aligned} A &\rightarrow \alpha B \mid \gamma_1 \mid \gamma_2 \mid \dots \mid \gamma_j . \\ B &\rightarrow \beta_1 \mid \beta_2 \mid \dots \mid \beta_n \end{aligned}$$

11	<u>Factor</u>	\rightarrow	<u>name</u>
12		$ $	<u>name</u> [ArgList]
13		$ $	<u>name</u> (ArgList)
15	<u>ArgList</u>	\rightarrow	Expr MoreArgs
16	<u>MoreArgs</u>	\rightarrow	, Expr MoreArgs
17		$ $	ϵ

F \rightarrow name F'

F' \rightarrow ϵ

F' \rightarrow [ArgList]

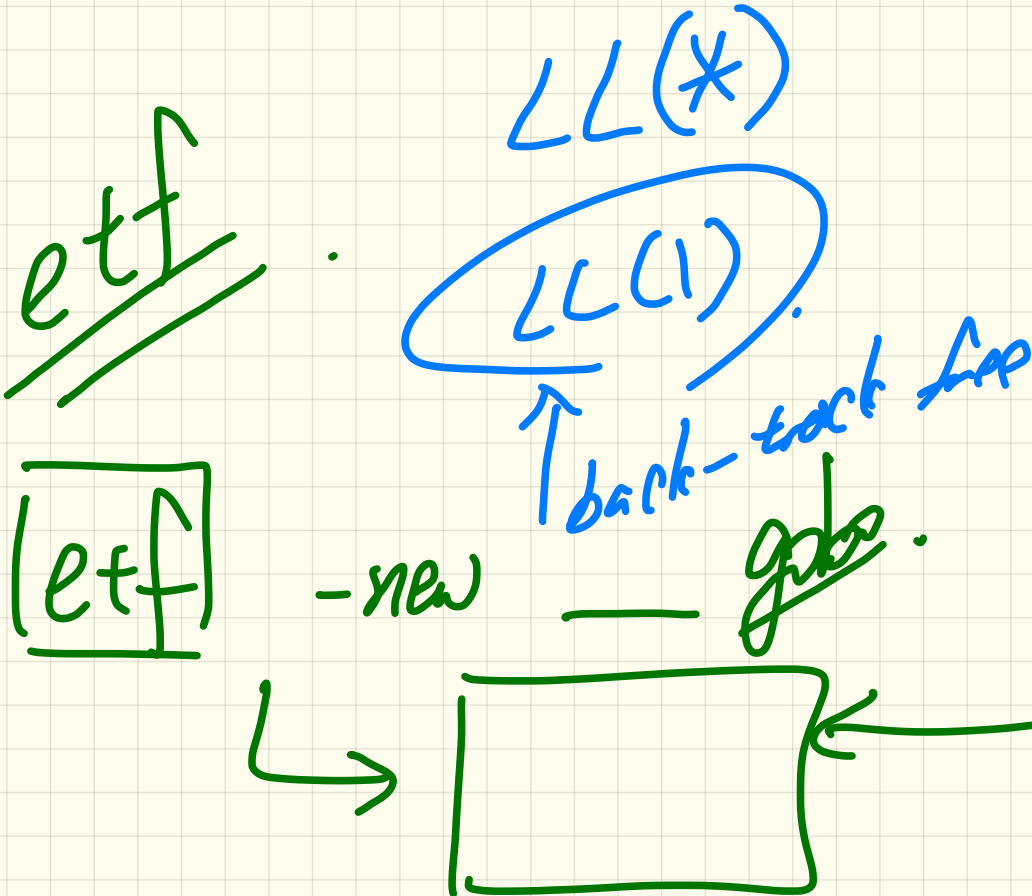
F' \rightarrow (ArgList)

Implementing a Recursive-Descent Parser

generated by ANTLR4!

	Production	FIRST ⁺
2	$Expr' \rightarrow + Term Expr'$	$\{+\}$
3	$ - Term Expr'$	$\{-\}$
4	$ \epsilon$	$\{\epsilon, eof, _)\}$

```
ExprPrim()  
  if word = + ∨ word = - then /* Rules 2, 3 */  
    word := NextWord()  
    if Term()  
      then return ExprPrim()  
      else return false  
    elseif word = ) ∨ word = eof then /* Rule 4 */  
      return true  
    else  
      report a syntax error  
      return false  
    end  
  Term()  
  ...
```



$$\textcircled{L} \rightarrow \underline{Ra}$$

$$\underline{R} \rightarrow \underline{aba}$$

$$Q \rightarrow \underline{bbc}$$

$$| \quad Q \quad ba$$

$$| \quad \underline{caba}$$

$$| \quad \underline{bc}$$

$$| \quad \underline{R} \quad bc$$



Common prefix

	alternativ	First	Intersection
L	Ra Qba	i	\emptyset
R			
R'			
\emptyset			
Q'			

left recursion

$$\underline{R} \rightarrow \underline{abaR'} \quad | \quad \underline{cabaR'}$$

$$\underline{R'} \Rightarrow \underline{bcR'}$$

$$| \quad \epsilon$$

$$\textcircled{Q} \Rightarrow \underline{bQ'}$$

$$\underline{Q'} \rightarrow \underline{bc}$$

$$| \quad c$$